Quiz 1 Makeup, MATH 240, Fall 2023 Write your name clearly.

Name:

Section Number:

UID:

(1) [20] **Using elementary row operations,** determine if the system of linear equations has a solution or not. If it does, find an explicit solution. If it does not have a solution, briefly explain why.

$$x_{1} - 3x_{2} + 4x_{3} = 3$$

$$3x_{1} - 7x_{2} + 7x_{3} = 4$$

$$-4x_{1} + 6x_{2} + 2x_{3} = 6$$

$$\begin{bmatrix} 1 & -3 & 4 & | & 3 \\ 3 & -7 & 7 & | & 4 \\ -4 & 6 & 2 & | & 6 \end{bmatrix} \xrightarrow{R_{2} - 3R_{1}} \begin{bmatrix} 1 & -3 & 4 & | & 3 \\ 0 & 2 & -5 & | & -5 \\ 0 & -6 & 1 & 8 & | & 1 \\ 0 & -6 & 1 & 8 & | & 1 \\ R_{1} - 2R_{3} & \begin{bmatrix} 1 & -3 & 4 & | & 3 \\ 0 & 2 & -5 & | & -5 \\ 0 & 1 & -3 & | & -3 \\ 0 & 0 & 1 & | & 1 \\ 0 & 1 & -3 & | & -3 \\ R_{1} + 3R_{2} & \begin{bmatrix} 1 & 0 & -5 & | & -6 \\ 0 & 0 & 1 & | & 1 \\ 0 & 1 & -3 & | & -3 \\ R_{1} + 3R_{2} & \begin{bmatrix} 1 & 0 & 0 & | & -1 \\ 0 & 0 & 1 & | & 1 \\ 0 & 1 & -3 & | & -3 \\ R_{1} + 3R_{2} & \begin{bmatrix} 1 & 0 & 0 & | & -1 \\ 0 & 0 & 1 & | & 1 \\ R_{3} + 3R_{2} & \begin{bmatrix} 1 & 0 & 0 & | & -1 \\ 0 & 0 & | & 0 \\ 0 & \end{bmatrix} \xrightarrow{R_{1} + 5R_{1}} x_{1} = 0 , x_{2} = 1$$